

MATHEMATICAL MODELING OF DIETARY AND CALORIC RESTRICTION INFLUENCE ON MEXFLY LONGEVITY

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EXPERIMENT

	DILUTION											
	100%		75%		50%		25%		10%		0%	
	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>
SUGAR	28.2	3.8	30.1	6.7	31.1	7.1	33.4	4.7	36.8	7.6	4.0	0.0
24 : 1	45.5	25.3	49.9	16.6	51.8	18.0	57.4	25.0	48.0	48.3	4.0	0.0
9 : 1	55.6	178.6	64.5	221.0	63.4	239.4	67.2	281.8	46.8	201.8	4.1	0.0
3 : 1	51.3	875.3	52.4	890.8	55.2	1085.7	53.9	866.5	30.0	191.4	3.9	0.0

MAXIMAL LIFE EXPECTANCY

	DILUTION											
	100%		75%		50%		25%		10%		0%	
	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>	e_0	<i>eggs</i>
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MAXIMAL REPRODUCTION

	DILUTION											
	100%		75%		50%		25%		10%		0%	
	e_0	eggs	e_0	eggs	e_0	eggs	e_0	eggs	e_0	eggs	e_0	eggs
SUGAR	28.2	3.8	30.1	6.7	31.1	7.1	33.4	4.7	36.8	7.6	4.0	0.0
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CONCENTRATIONS

	DILUTION											
	100%		75%		50%		25%		10%		0%	
	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>
SUGAR	33.0	0	25.0	0	16.7	0	8.3	0	3.3	0	0	0
24 : 1	32.1	1.3	24.0	1.0	16.0	0.7	8.0	0.3	3.2	0.1	0	0
9 : 1	30.0	3.3	22.5	2.5	15.0	1.7	7.5	0.8	3.0	0.3	0	0
3 : 1	25.0	8.3	18.8	6.2	12.5	4.2	6.2	2.1	2.5	0.8	0	0

CONCENTRATIONS

maximal life expectancy

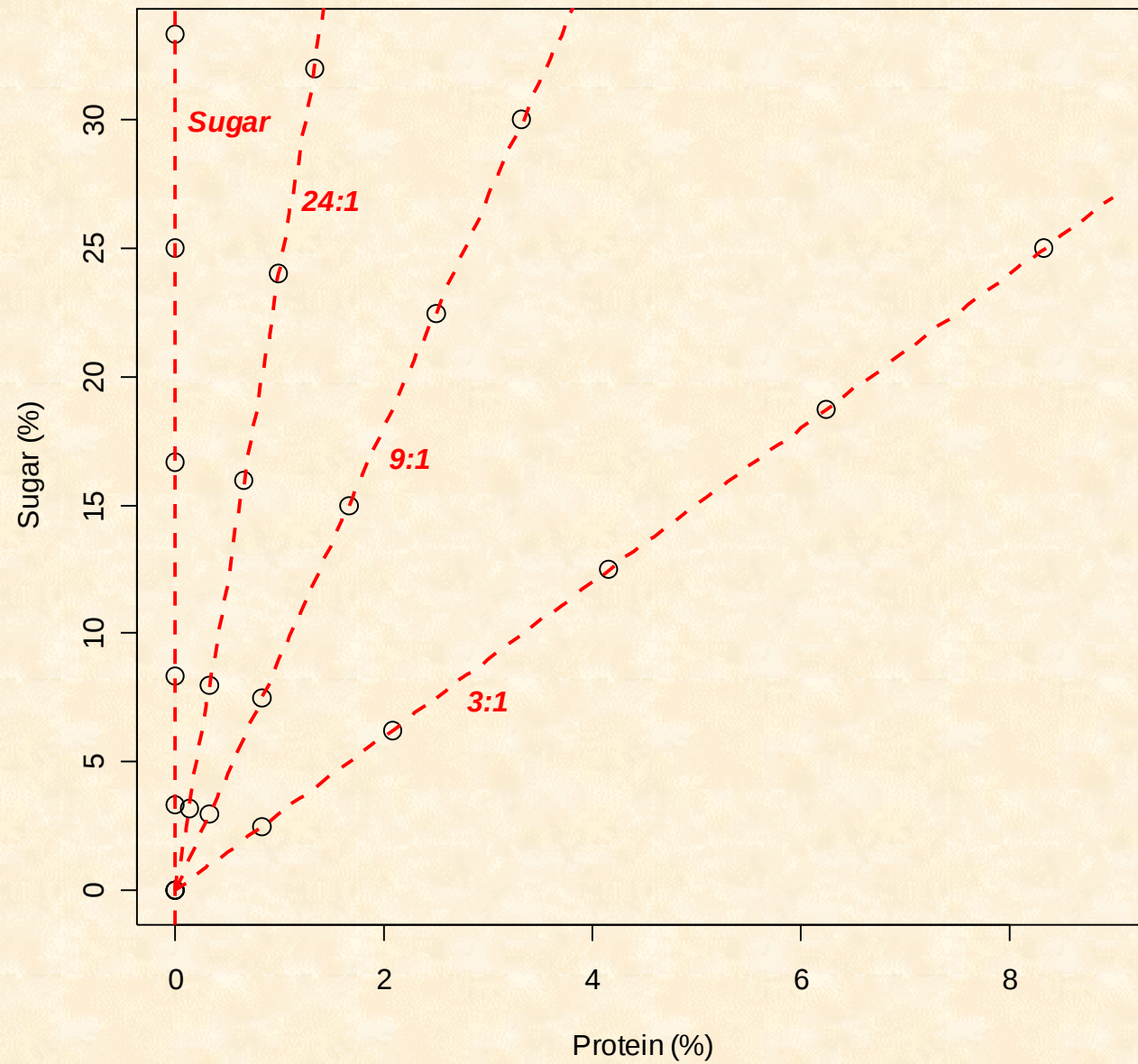
	DILUTION											
	100%		75%		50%		25%		10%		0%	
	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>
SUGAR	33.0	0	25.0	0	16.7	0	8.3	0	3.3	0	0	0
24 : 1	32.1	1.3	24.0	1.0	16.0	0.7	8.0	0.3	3.2	0.1	0	0
9 : 1	30.0	3.3	22.5	2.5	15.0	1.7	7.5	0.8	3.0	0.3	0	0
3 : 1	25.0	8.3	18.8	6.2	12.5	4.2	6.2	2.1	2.5	0.8	0	0

CONCENTRATIONS

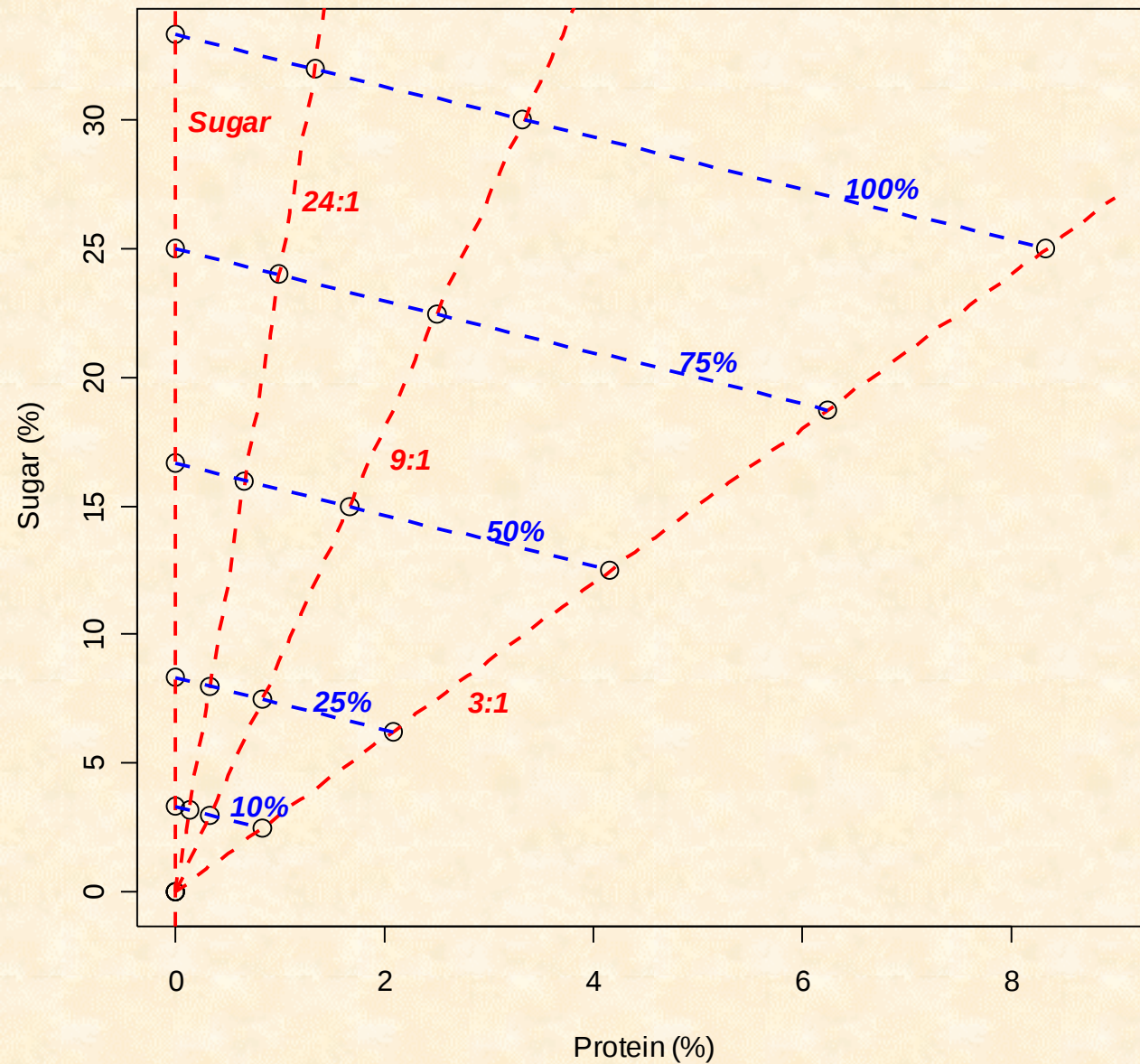
maximal reproduction

	DILUTION											
	100%		75%		50%		25%		10%		0%	
	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>	<i>Sug</i>	<i>Prot</i>
SUGAR	33.0	0	25.0	0	16.7	0	8.3	0	3.3	0	0	0
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9 : 1	30.0	3.3	22.5	2.5	15.0	1.7	7.5	0.8	3.0	0.3	0	0
3 : 1	25.0	8.3	18.8	6.2	12.5	4.2	6.2	2.1	2.5	0.8	0	0

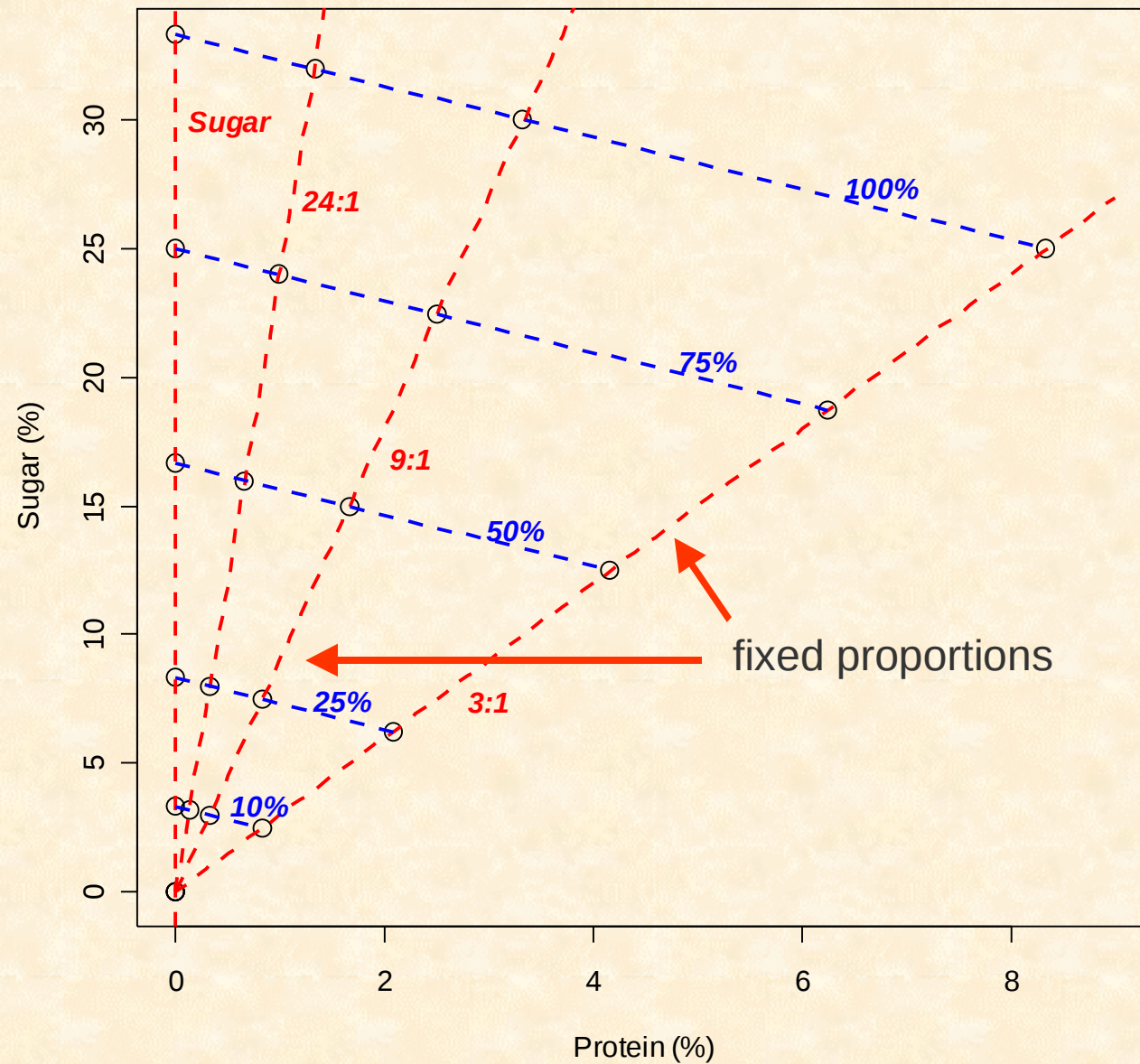
CONCENTRATIONS



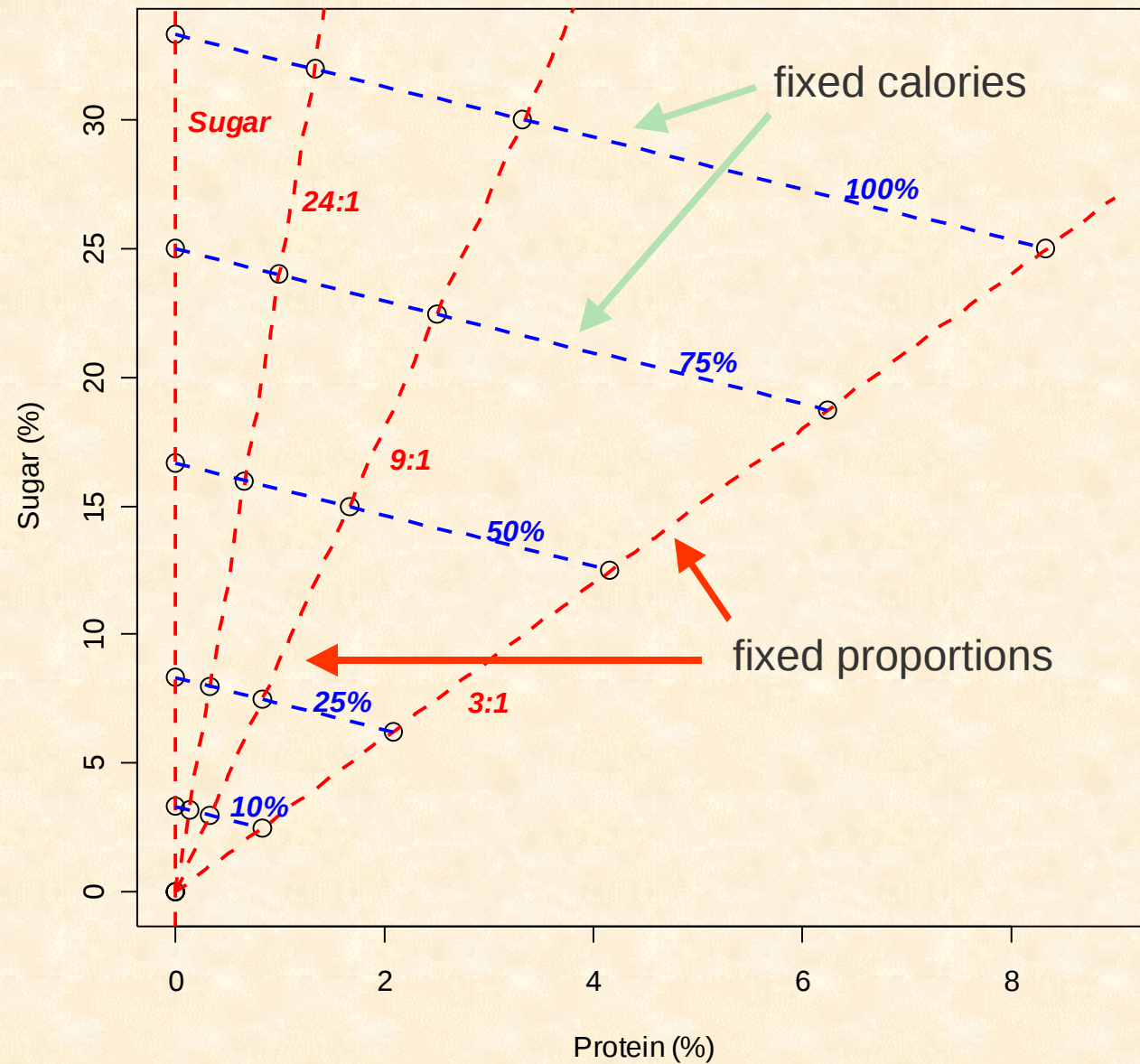
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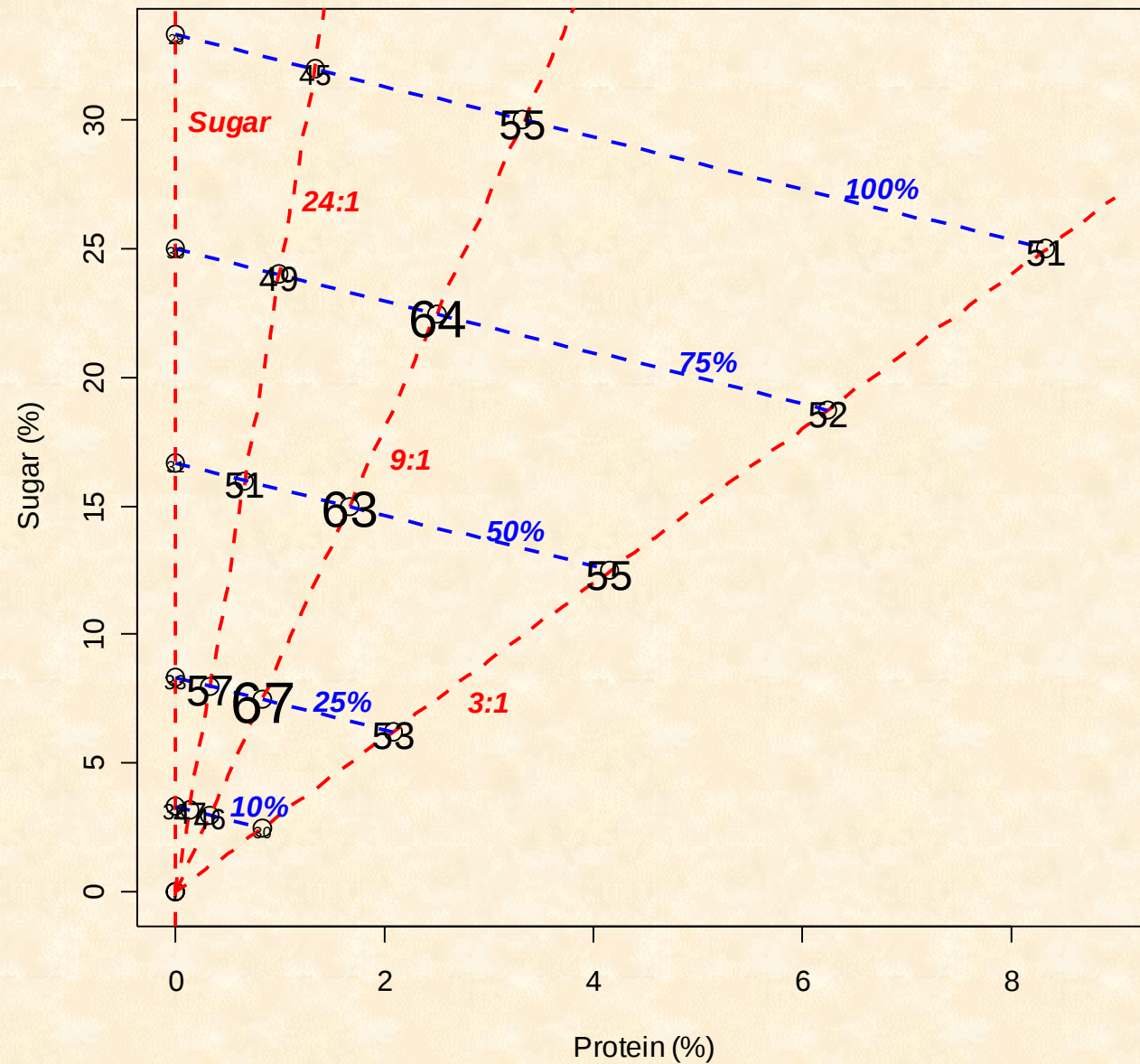
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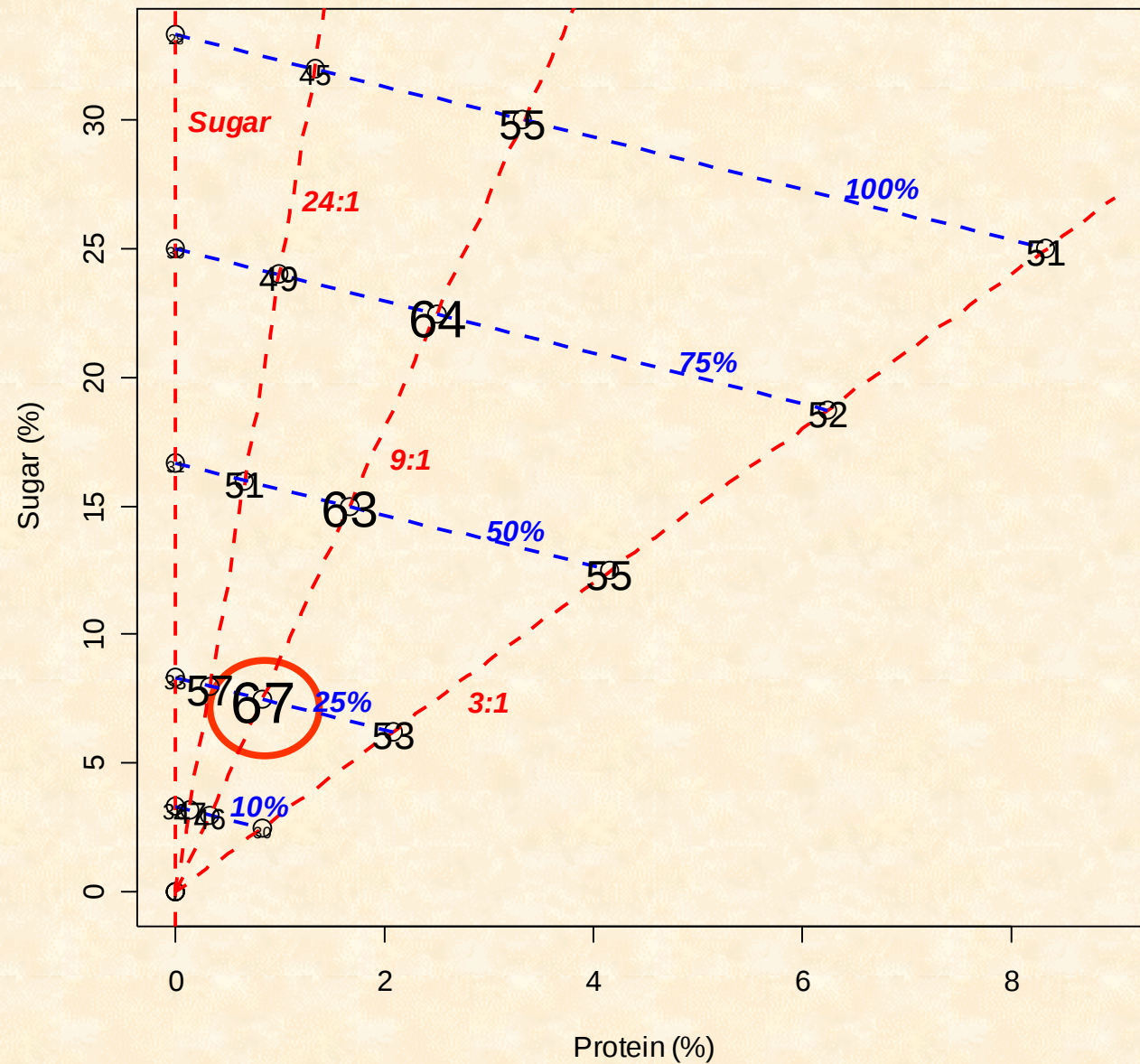
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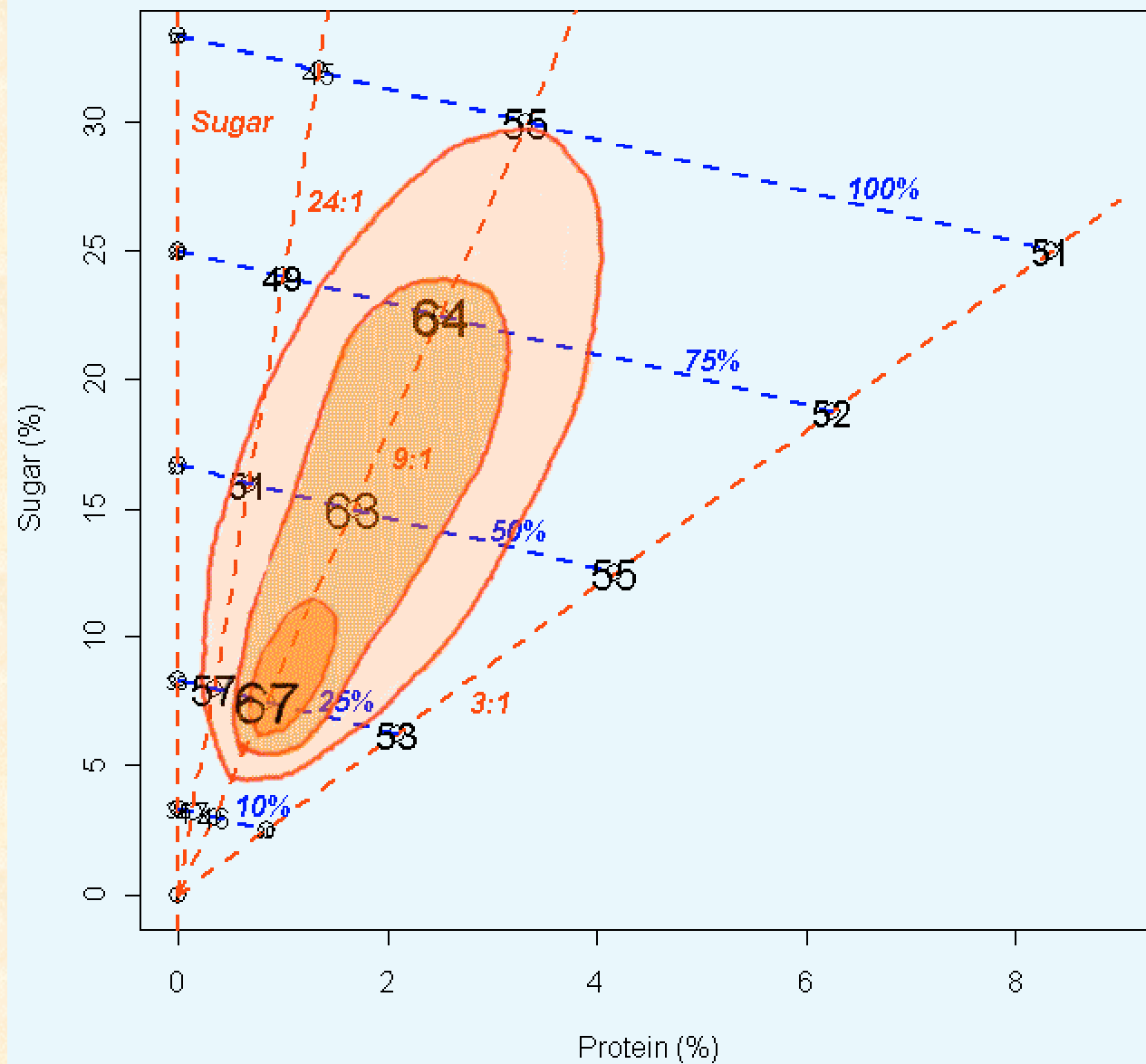
MEAN LIFE SPAN



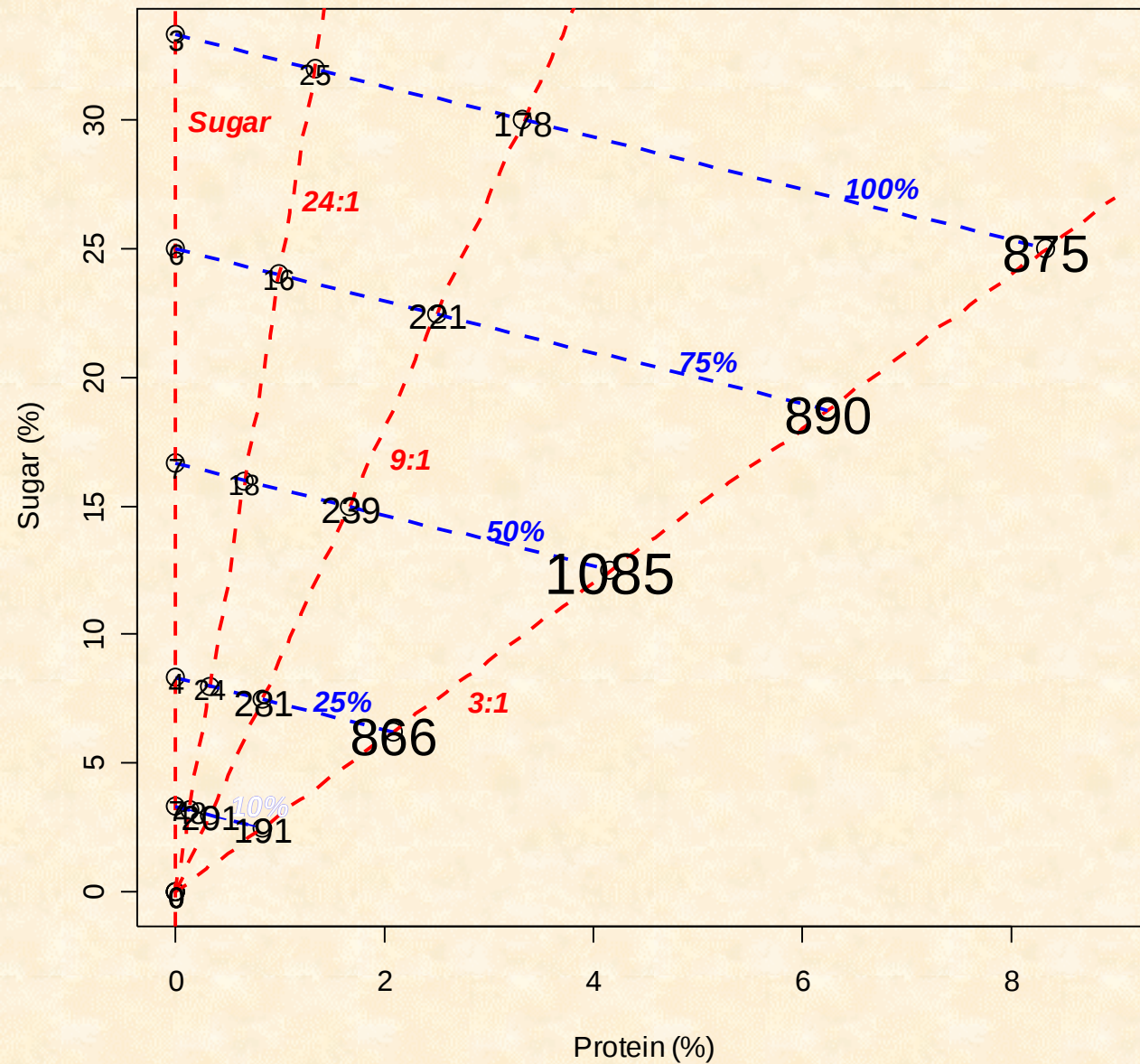
MEAN LIFE SPAN



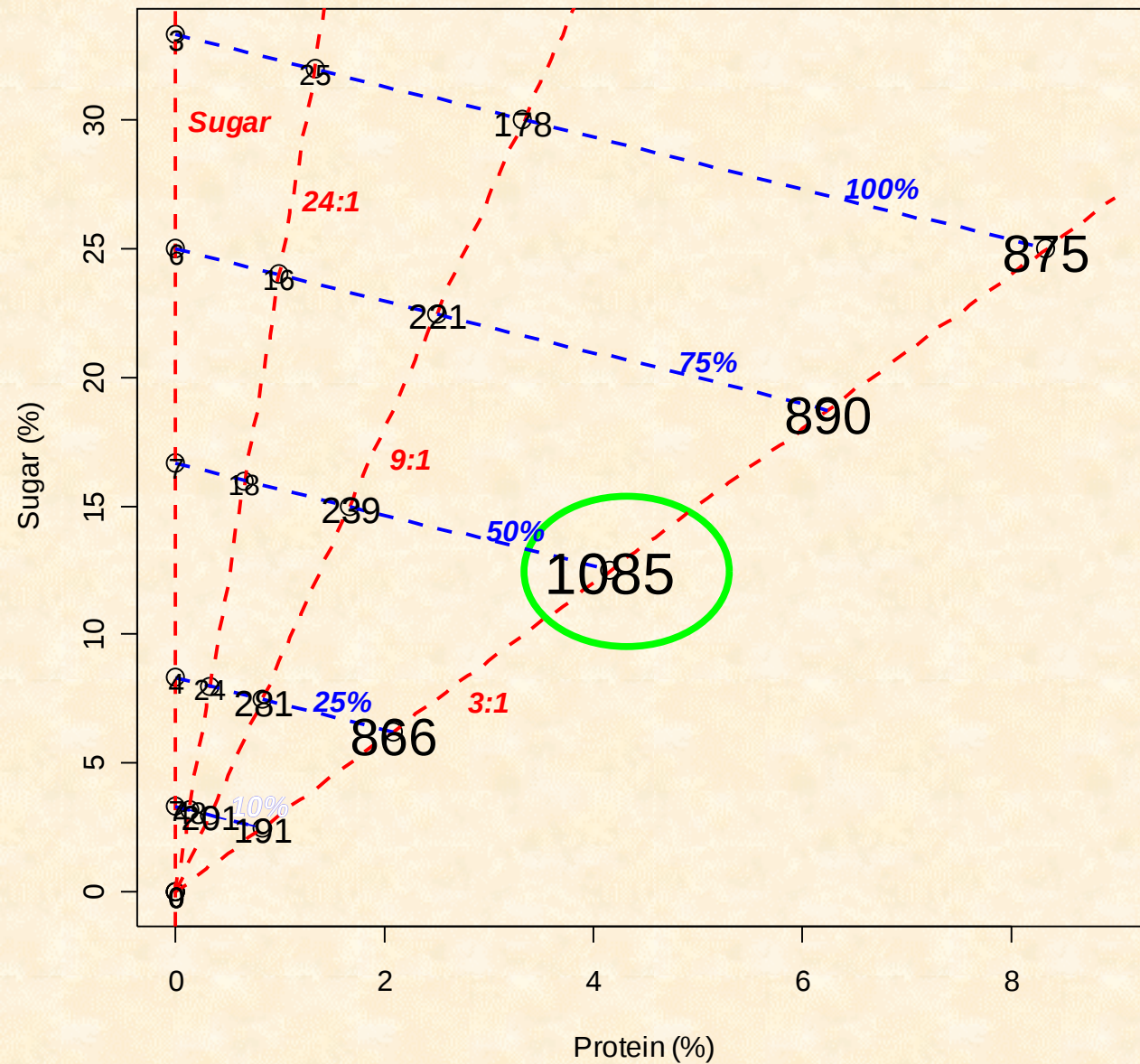
MEAN LIFE SPAN



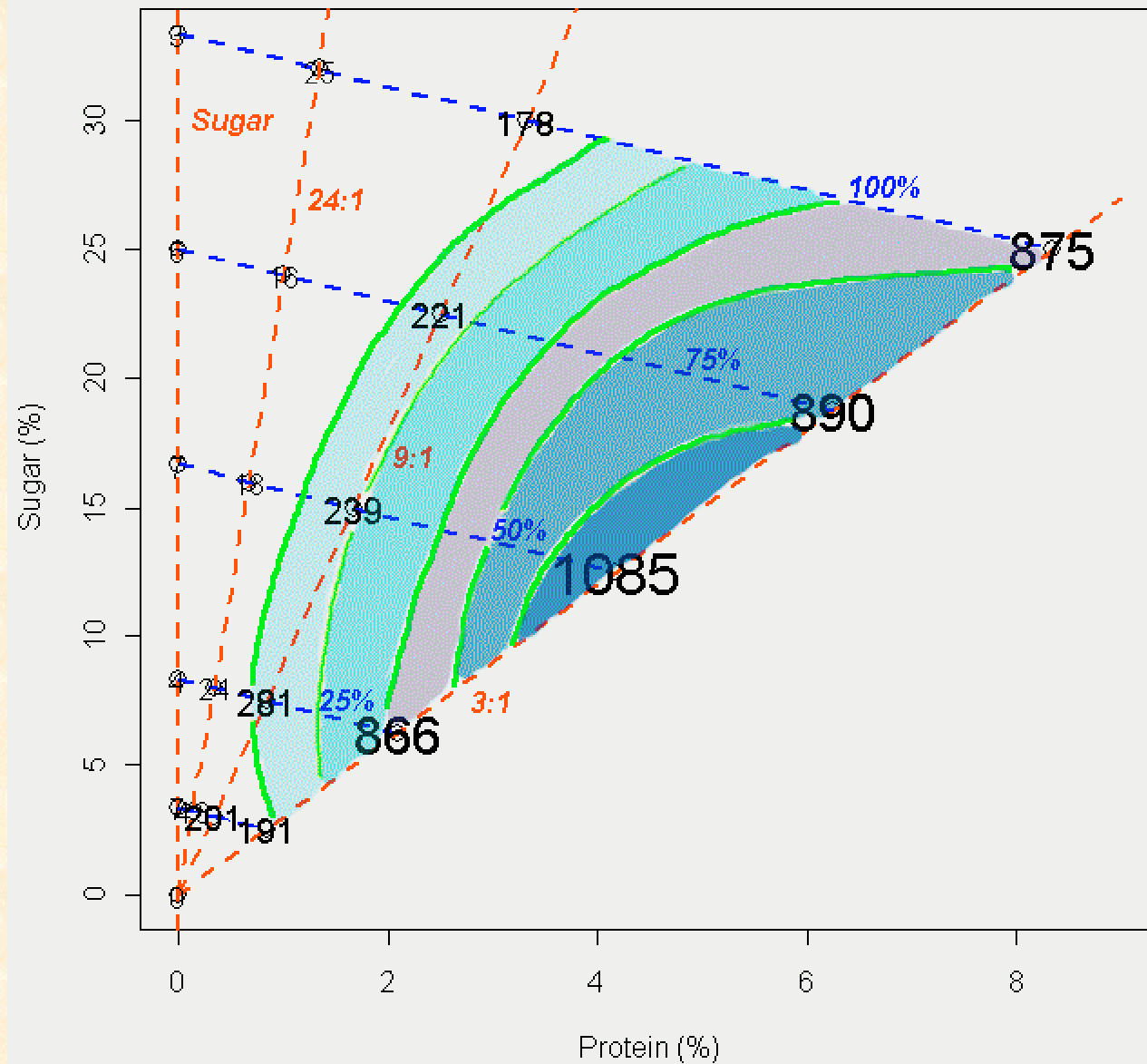
REPRODUCTION



REPRODUCTION



REPRODUCTION



Reproduction depends
both on calorie intake and
protein concentration

ENERGY FOR REPRODUCTION MODELING

$$E_r = E_p - k_1 E_m f(E_p)$$

Energy allocated for reproduction proportional to the amount of protein in food minus amount of protein spent for reparation of damages

ENERGY FOR REPRODUCTION MODELING

$$E_r = E_p - k_1 E_m f(E_p)$$

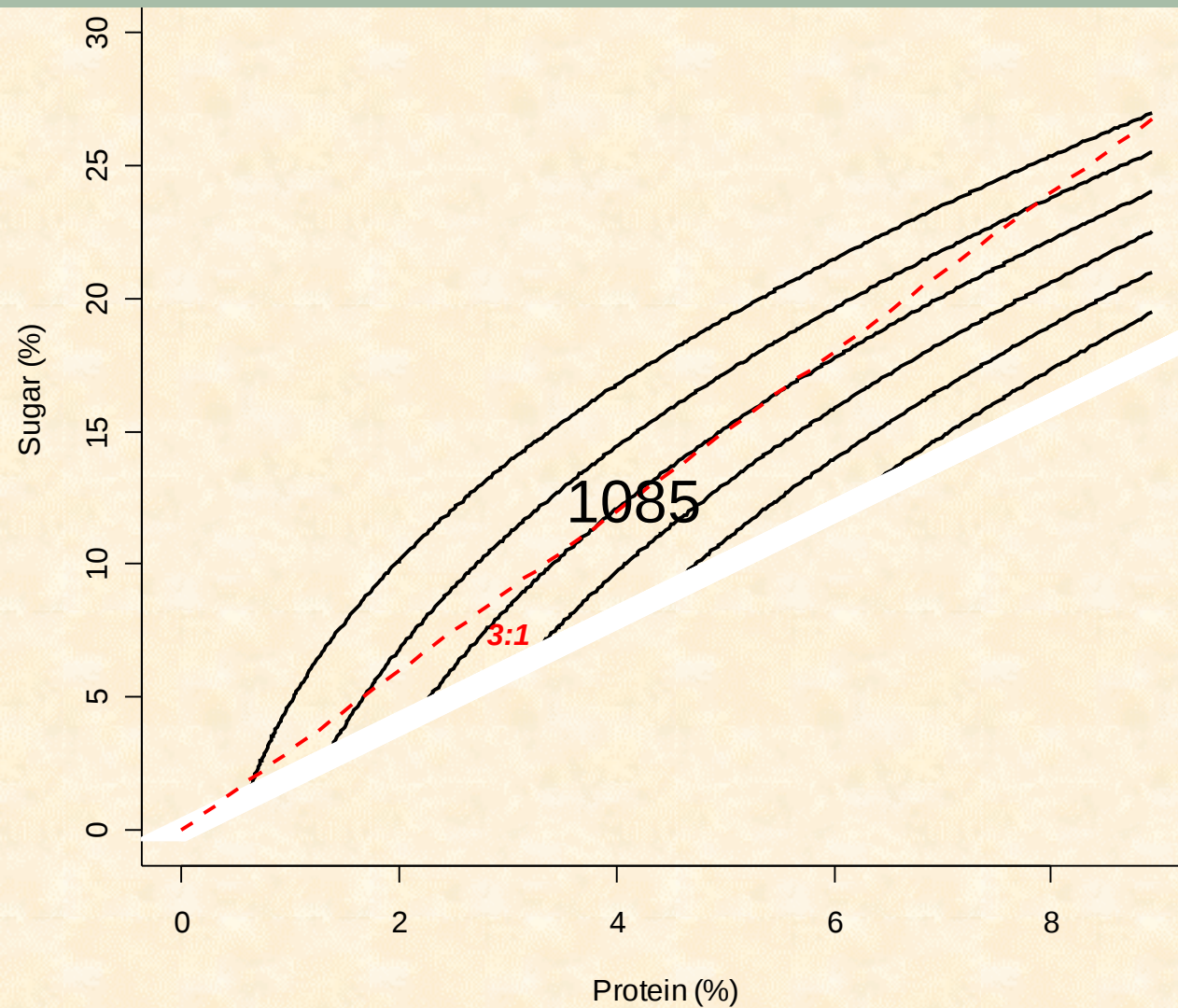
$$E_m = E_s - l_1 E_r j(E_s)$$

Energy allocated for maintenance proportional to the amount of sugar in food minus amount of sugar spent for reproduction

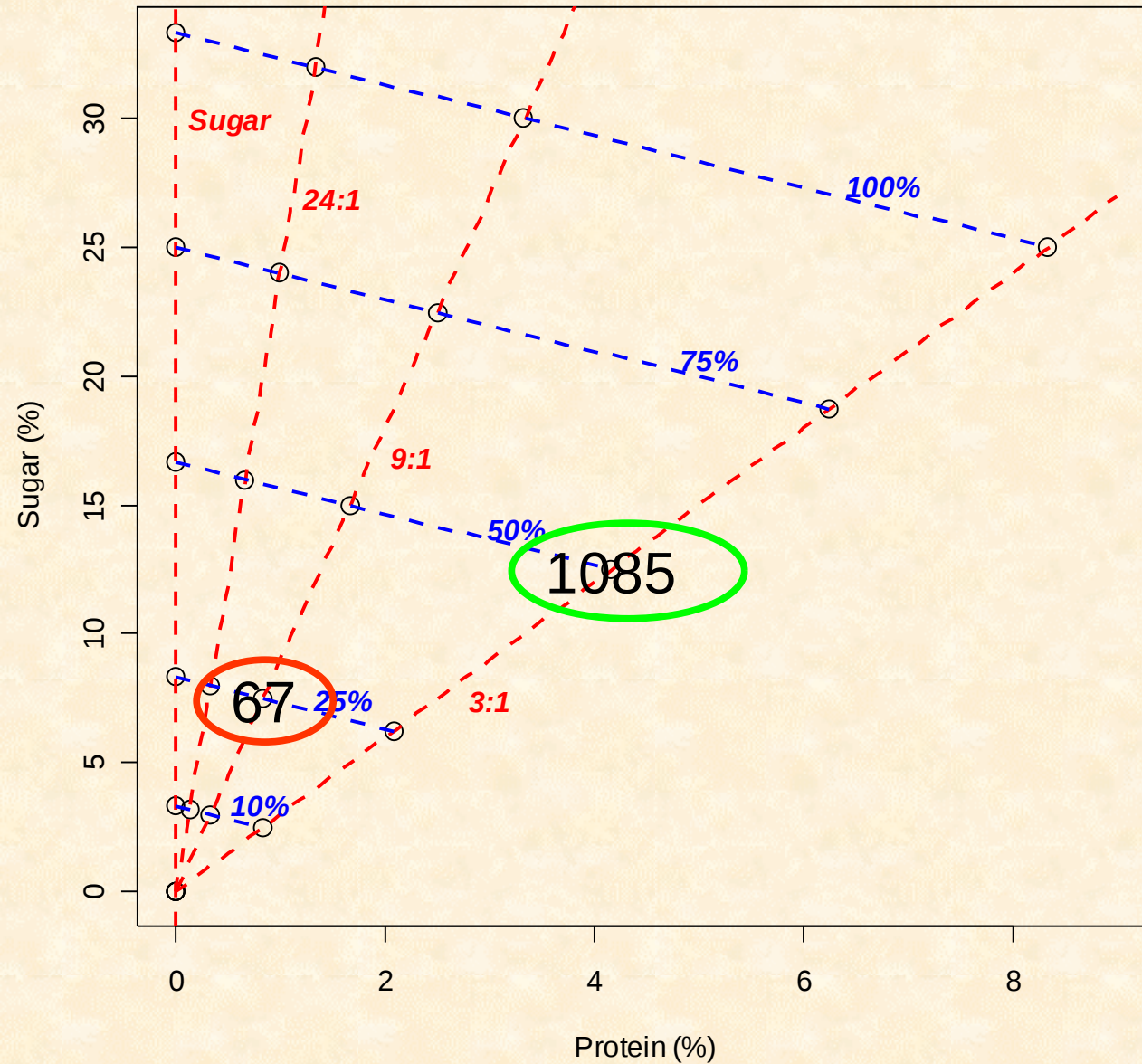
ENERGY FOR REPRODUCTION MODELING

$$E_r = \frac{E_p - k_1 f(E_p) E_s}{1 - k_1 l_1 f(E_p) j(E_s)}$$

ENERGY FOR REPRODUCTION MODELING *EXAMPLE*



REPRODUCTION vs. MEAN LIFE SPAN



LONGEVITY MODELING

Mortality model

$$m(x) = a \exp(bx)$$

LONGEVITY MODELING

Mortality model

$$m(x) = a \exp(bx)$$

Strehler and Mildvan model

$$a = K \exp(-V_0 / e) \quad b = V_0 B / e$$

Vitality

$$V(x) = V_0 (1 - Bx)$$

LONGEVITY MODELING

Mortality model

$$V_0 = E_m$$

$$m(x) = a \exp(bx)$$

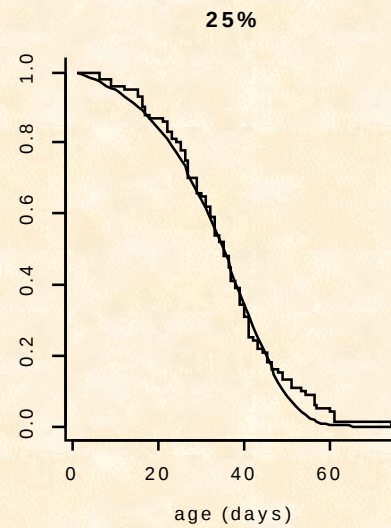
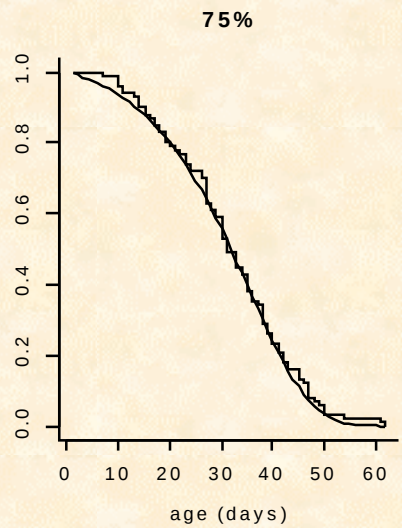
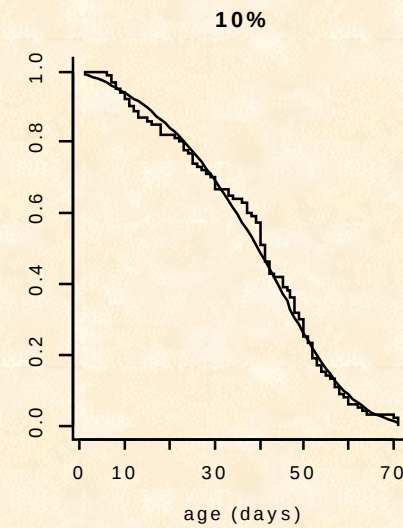
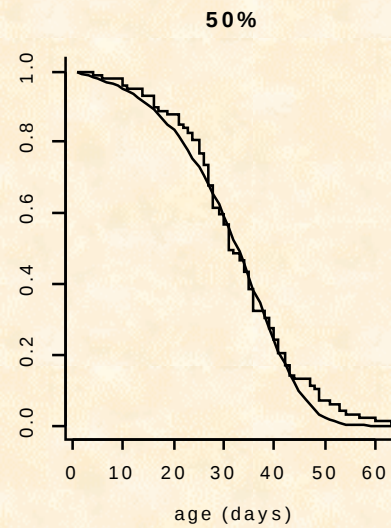
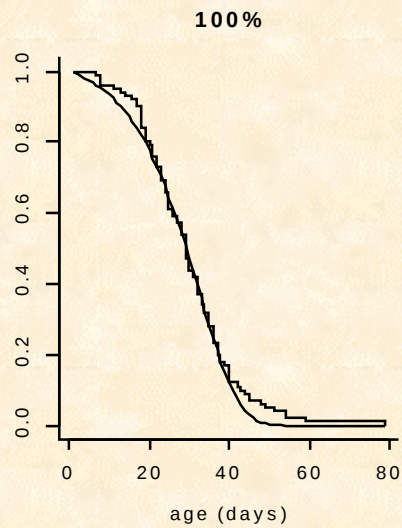
Strehler and Mildvan model

$$a = K \exp(-V_0 / e) \quad b = V_0 B / e$$

Vitality

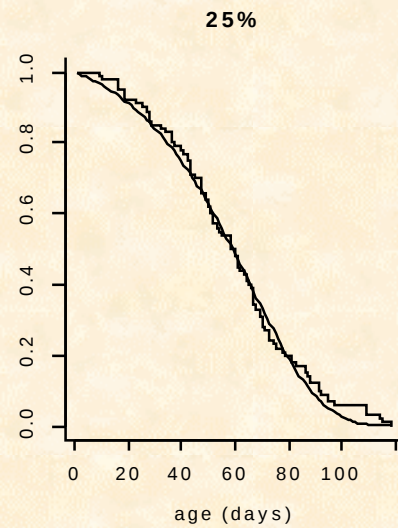
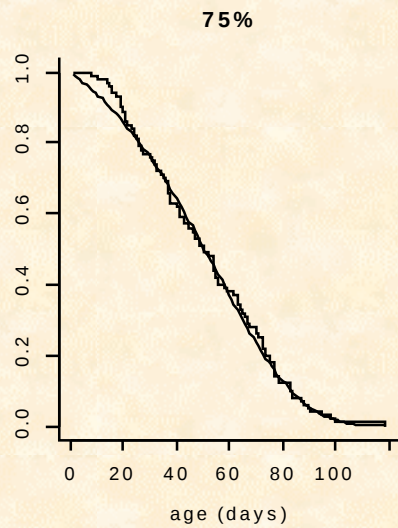
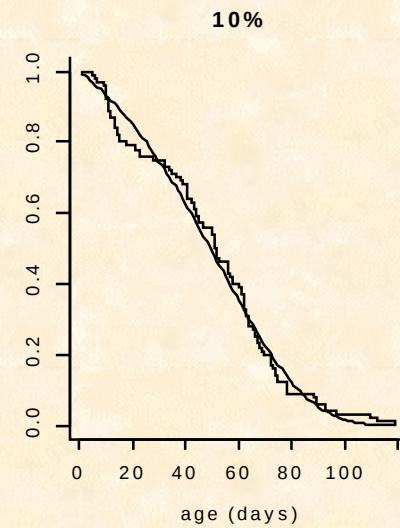
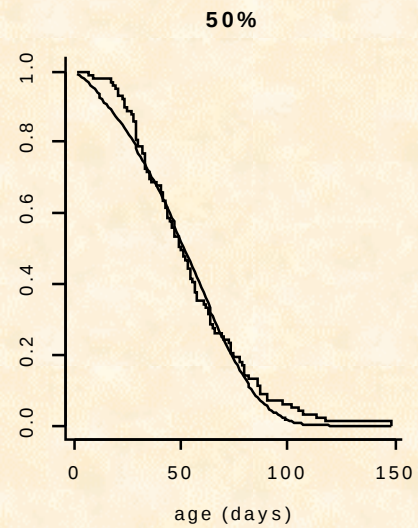
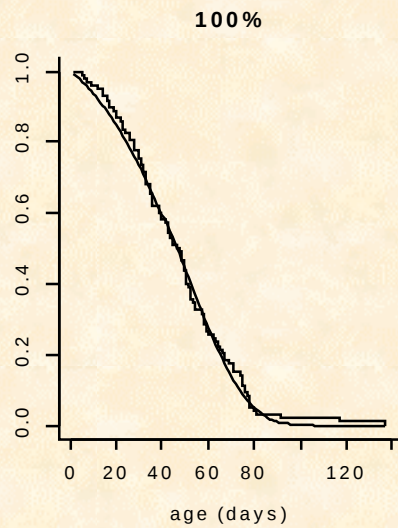
$$V(x) = V_0 (1 - Bx)$$

LONGEVITY MODELING *RESULTS*



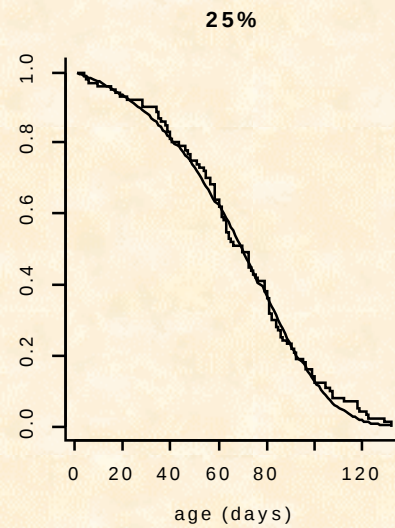
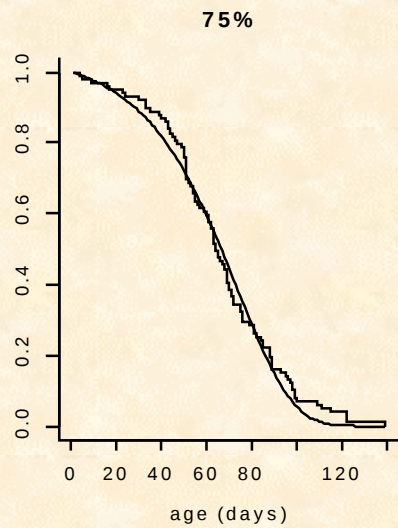
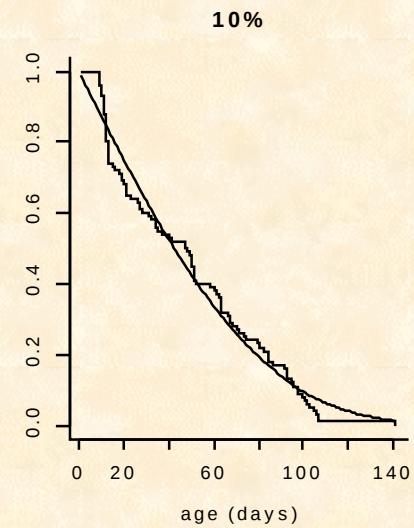
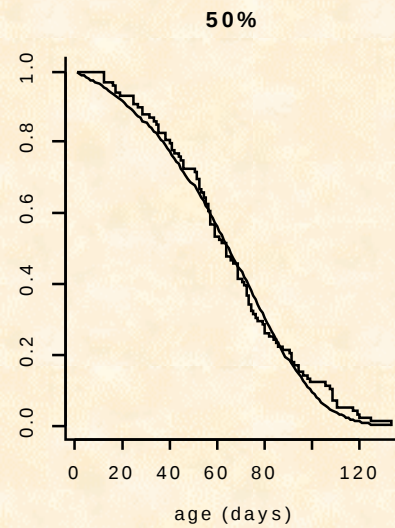
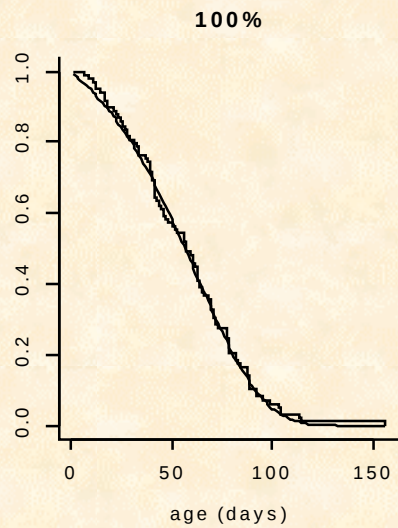
Sugar

LONGEVITY MODELING *RESULTS*



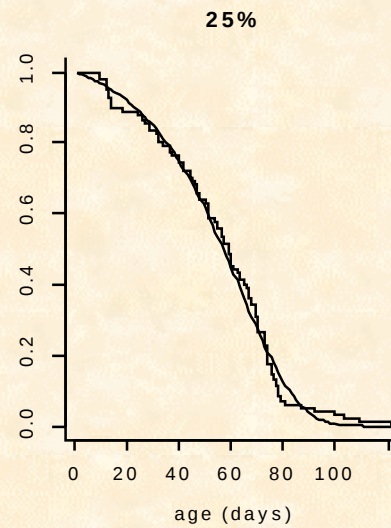
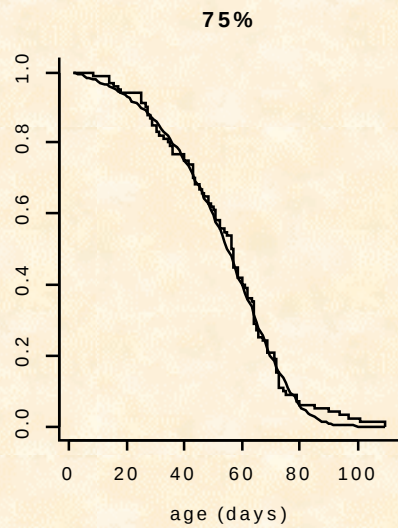
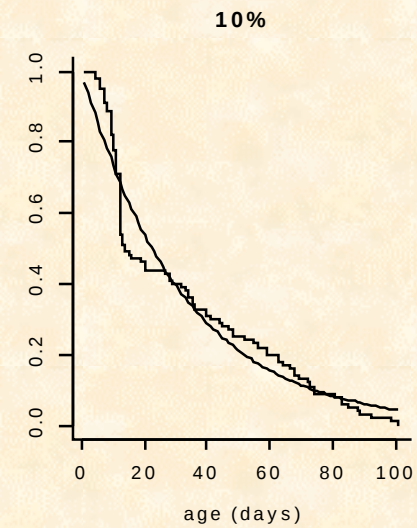
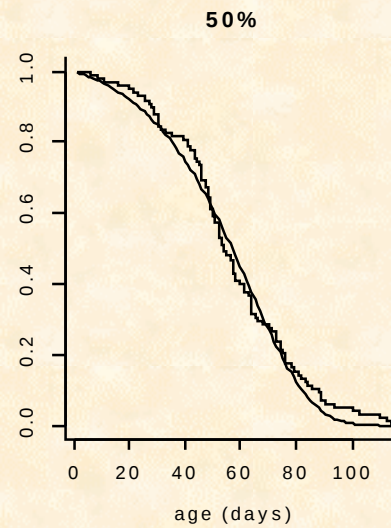
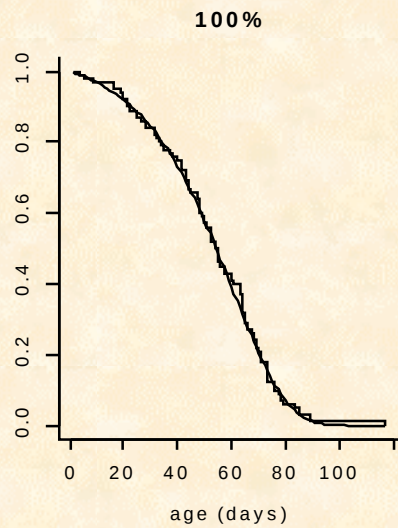
24:1

LONGEVITY MODELING *RESULTS*



9:1

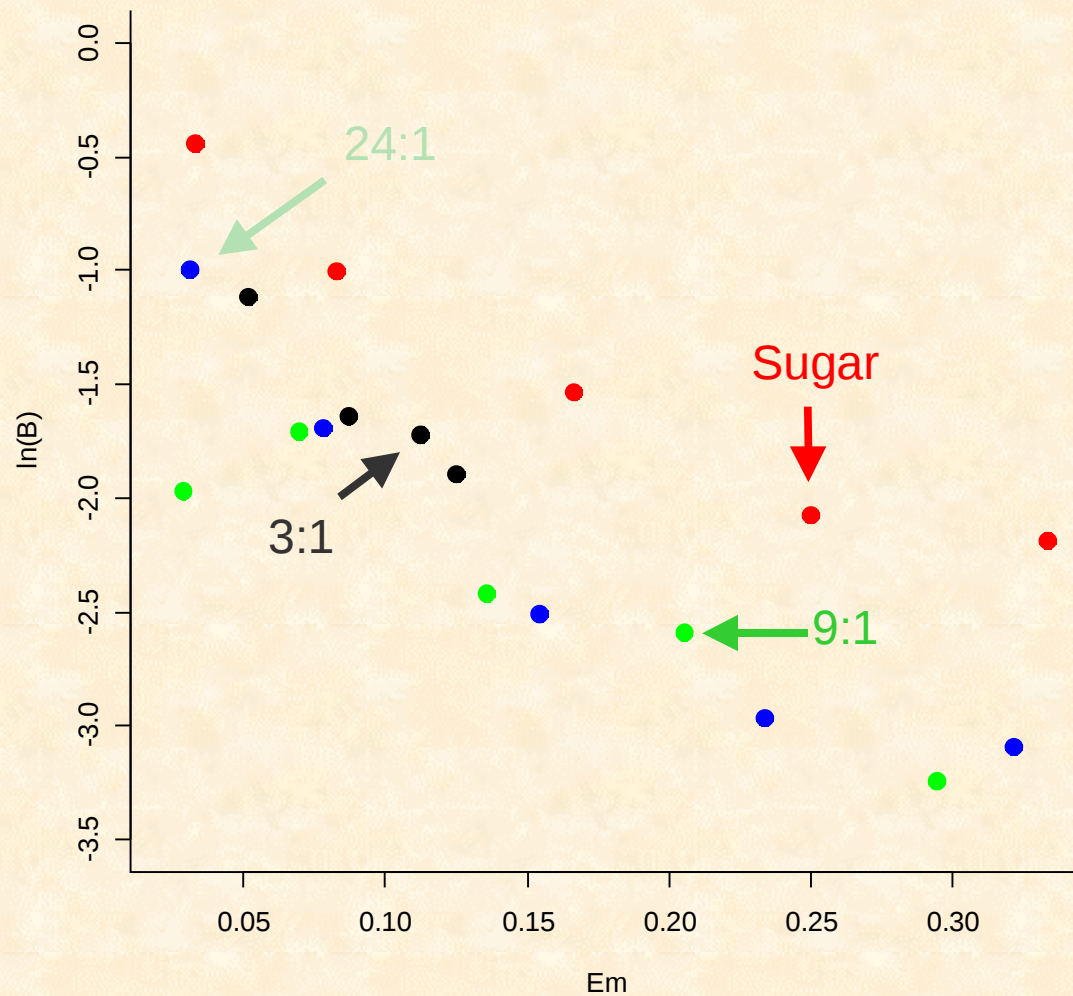
LONGEVITY MODELING *RESULTS*



3:1

LONGEVITY MODELING

RESULTS: $\ln B(E_m)$



CONCLUSIONS

- § Calorie intake is not the main factor in the longevity extension
- § Life span is extended to a greater extent by reducing protein concentration than by reducing sugar concentration
- § Rate of vitality decline with age decreases with increase of energy spent for maintenance